

1 Laboratory-based Vis–NIR spectroscopy and partial least square regression with  
2 spatially correlated errors for predicting spatial variation of soil organic matter  
3 content

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9

10 **Abstract**

11 Soil organic matter (SOM) has beneficial effects on soil properties for plant growth and production. Moreover, SOM  
12 changes carbon dioxide concentrations in the atmosphere and can influence climate warming. Conventional methods for  
13 SOM determination based on laboratory analyses are costly and time consuming. Use of soil reflectance spectra is an  
14 alternative approach for SOM estimation and has the advantage of being rapid, non-destructive and cost effective. This  
15 method assumes that residuals are independent and identically distributed. However, in most cases this assumption does  
16 not hold owing to spatial dependence in soil samples. The aim of the paper was to test the potential of laboratory Vis–  
17 NIR spectroscopy to develop an approach of partial least square regression (PLSR) with correlated errors for estimating  
18 spatially varying SOM content from laboratory-based soil Vis–NIR spectra and producing a continuous map using a  
19 geostatistical method.

20 The study area was the Turbolo watershed (Calabria, southern Italy), which is representative of Mediterranean areas  
21 being highly susceptible to soil degradation. Topsoil samples were collected at 201 locations. To reduce the lack of  
22 linearity that may exist in the spectra, reflectance (R) spectra were transformed in absorbance spectra ( $\log(1/R)$ ).  
23 Partial least squared regression (PLSR) analysis was then used to predict SOM from reflectance spectra. To take into  
24 account spatial correlation between observations, the significant latent variables from PLSR were used as regressors in  
25 a linear mixed effect model with correlated errors of SOM. The spatial approach and traditional PLSR were compared  
26 through the calculation of root mean square prediction error (RMSPE). In order to produce a continuous map, the  
27 estimated SOM data were interpolated by ordinary kriging. The approach is particularly advantageous when the data  
28 exhibit a pronounced spatial autocorrelation and could be used in digital soil mapping.

29

30

## 1    1.    *Introduction*

2

3    Soil organic matter (SOM) is a key attribute of soil and environmental quality because it is an important sink and  
4    source of main plant and microbial nutrients (Nieder and Benbi, 2008). Moreover, SOM exerts an important  
5    influence on the physical, chemical and biological properties and functions of soil (McBratney et al., 2014; Nieder  
6    and Benbi, 2008), because its depletion may reduce aggregate stability, resulting in crusting and compaction, as  
7    well as nutrient supply (Mabit and Bernard, 2009). Moreover, organic matter increases the soil's nutrient cycling  
8    capability (McBratney et al., 2014) and provides a large pool of macronutrients such as nitrogen, phosphorous  
9    and sulfur, which are very important for soil fertility. In addition, SOM has a positive influence on water  
10    retention capacity, porosity and cation exchange capacity (CEC).

11    On the global scale, carbon stored in soils represents one of the largest reservoirs of organic carbon and  
12    consequently, by either sequestering or releasing carbon in the atmosphere, soil can alter the terrestrial carbon  
13    balance and thereby the greenhouse effect (Lal, 2004; Lützow et al., 2006).

14    In recent decades, visible, near-infrared (Vis–NIR) reflectance spectroscopy has been found to be useful in  
15    measuring soil properties because the techniques are rapid, relatively inexpensive, and require minimal sample  
16    preparation and no hazardous chemicals; furthermore, they are non-invasive and several soil properties can be  
17    measured from a single scan (e.g. Demattê et al., 2006; McBratney et al., 2006; Reeves et al., 2001, 2002;  
18    Shepherd and Walsh, 2002; Stenberg et al., 2010; Viscarra Rossel et al., 2006).

19    There is widespread interest in Vis–NIR reflectance spectroscopy, even though soil Vis–NIR spectra are largely  
20    non-specific, resulting from overlapping absorptions of constituents often present in small concentrations in the  
21    soil (Viscarra Rossel and Behrens, 2010). The method is based on the simplified assumption that the soil  
22    reflectance in the 350–2500 nm spectral region is a linear combination of the spectral signatures of its  
23    compositional components weighted by their abundance (Ben-Dor, 2002; Curran, 1994; Ge et al., 2007).

24    Therefore, changes in the chemical, physical and mineralogical properties of the soil produce distinct spectral  
25    features that can be detected through reflectance spectroscopy (Aïchi et al., 2009; Conforti et al., 2013a; Nanni  
26    and Demattê, 2006; Shepherd and Walsh, 2002; Viscarra Rossel et al., 2006). In particular, soil reflectance  
27    spectra are heavily dependent on SOM, as well as on other properties such as soil moisture and texture (Aïchi et  
28    al., 2009; Stevens et al., 2008).

29    Vis–NIR reflectance spectroscopy requires only a few seconds to measure a soil sample, but the relevant  
30    information needs to be mathematically extracted from the spectra so that it can be correlated with soil

1 properties. To analyze soil reflectance spectra chemometrics techniques and multivariate calibrations (Martens  
2 and Næs, 1989; Stenberg et al., 2010; Viscarra Rossel and Behrens, 2010), such as multiple linear regression  
3 (MLR), principal components regression (PCR), partial least-squares regression (PLSR) and artificial neural  
4 networks (ANN) (e.g. Aïchi et al., 2009; Conforti et al., 2013b; Farifteh et al., 2007; Shepherd and Walsh, 2002;  
5 Viscarra Rossel et al., 2006) are generally used.

6 However, these techniques assume that SOM residuals (measured SOM minus predicted SOM) are identically and  
7 independently distributed: in other words, SOM observations should be independent of each other to guarantee  
8 optimality of the prediction model (Ge et al., 2007). Since soil properties generally exhibit significant spatial  
9 correlation with different degrees of spatial dependence, the use of PLSR combined with a linear mixed effect  
10 model (LMEM) (Lark, 2009; Stein, 1999) is expected to produce more accurate estimates. LMEM uses the  
11 significant latent variables from PLSR as fixed effects and the spatial covariance function of residuals as the  
12 stochastic (random) component to predict SOM.

13 Moreover, in the perspective of site-specific management, SOM content needs to be estimated spatially in order  
14 to produce accurate continuous maps, which can improve the information on local variation required by land  
15 managers and farmers (Viscarra Rossel and McBratney, 1998). However, from this point of view, the combined  
16 approach still leaves the task unfinished because the SOM predictions are made only at the sampled locations. A  
17 geostatistical analysis allows to map the spatial pattern of SOM prediction (Brown et al., 2006; Mouazen et al.,  
18 2007; Sarkhot et al., 2011; Viscarra Rossel et al., 2011), which is much more informative than the map of sparse  
19 observations for estimating carbon storage in the soil.

20 The objective of the paper was to develop an approach of partial least square regression (PLSR) with correlated  
21 errors for estimating spatially varying soil organic matter from laboratory-based soil Vis-NIR spectra and  
22 producing a continuous map using a geostatistical method. To estimate SOM, PLSR was combined with a linear  
23 mixed effect model (LMEM), which used the significant latent variables from PLSR as fixed effects, whereas  
24 spatial correlation between residuals as stochastic (random) component.

25

## 26 2. *Materials and methods*

27

### 28 2.1. *Study area*

29

30 The study area was the Turbolo watershed, located in the north of Calabria (southern Italy) between 39°32'25"N

1 and 39°29'51"N latitude, 16°12'57"E and 16°05'21"E longitude (Fig. 1), and covers an area of 29.2 km<sup>2</sup>.  
2 Elevation ranges from 75 to 1015 m a.s.l., and slopes from 0° to 56.5°, then the landscape is characterized by  
3 large variability. The streams have a sub-dendritic drainage pattern, and the length of the main channel is about  
4 13 km.  
5 The climate is sub-humid, with average annual precipitation of 1200 mm and average air temperature of 16 °C  
6 (Conforti, 2009; Conforti et al., 2011). Rainfall mostly occurs from November to February, with frequent high-  
7 intensity rainstorms. The pedoclimatic regime is xeric and thermic, shifting to udic and mesic in the upper  
8 reaches (ARSSA, 2003).  
9 The western part of the Turbolo watershed is characterized by steep slopes shaped on Paleozoic metamorphic  
10 rocks (mainly gneiss and schist), intensely fractured and weathered and in many places covered by a thick  
11 regolith (Fig. 1). In a wide eastern part of the study area, the morphology is characterized by gentle slopes and  
12 terraces cut on sedimentary terrains of Neogene–Quaternary ages mostly clays, sands and conglomerates  
13 (Lanzafame and Zuffa, 1976).  
14 The main soil groups occurring in the study area (Fig. 2a), according to the soil map of Calabria (ARSSA, 2003),  
15 are Luvisols, Cambisols, Vertisols and Fluvisols (IUSS Working Group WRB, 2006).  
16 The soil profiles frequently appear truncated or severely degraded by water erosion and gravitational processes  
17 (Conforti et al., 2012; Conforti et al., 2014; Lucà et al., 2011; Scarciglia et al., 2012). The prevailing soil textural  
18 classes are sandy loam and sandy clay loam (Buttafuoco et al., 2012; Conforti, 2009).  
19 From the point of view of land use (Fig. 2b), about half of the study area is characterized by agriculture, mainly  
20 crops and olive groves, whereas more than 20% has a shrubby and herbaceous cover often left to pasture  
21 (Conforti, 2009). The remaining area consists of woodland, especially in the western part of the basin (Fig. 2b).  
22 Finally, erosion may be extreme on bare slopes.

23

## 24 2.2. *Soil sampling and analysis*

25

26 Composite soil samples were collected at 201 locations within the study area (Fig. 1) by using an auger sampler;  
27 soil sampling depth was set at 0.20 m, because this represents the most frequent value of A- horizon depth in the  
28 area.

29 The sampling sites were selected by subdividing the study area into 300 m × 300 m cells and within each of  
30 which, one point was chosen to be representative of the cell area on the basis of main soil–landscape features

1 (geological substrate, topographic characteristics, soil types, land use/cover and development/degradation  
2 conditions of the topsoil). The locations of the sampling sites were recorded with a GPS Garmin eTrex30, with an  
3 accuracy of 3–5 m.

4 To ensure a soil homogeneous mixture, soil samples were dried, ground and sieved at 2 mm prior to analysis.  
5 Each sample was then split into two sub-samples: one was used for the laboratory spectral measurements, while  
6 the determination of SOM content was conducted on the other sub-sample, by the Walkley–Black method (Sequi  
7 and De Nobili, 2000).

8

### 9 2.3. *Measurement and pre-treatment of Vis–NIR spectroscopy data*

10

11 Vis–NIR reflectance of soil samples was measured in the laboratory, under artificial light, using an ASD FieldSpec  
12 Pro 350–2500 nm spectroradiometer (Analytical Spectral Devices Inc., Boulder, Colorado, USA), which combines  
13 three spectrometers to cover the spectrum portion (350 and 2500 nm), with a sampling interval of 1.4 nm for  
14 the 350–1000 nm region and 2 nm for the 1000–2500 nm region. FieldSpec Pro provided output at spectral  
15 resolution of 1 nm through a weighted cubic spline algorithm for interpolation, thus producing 2151 spectral  
16 bands. Two 100 W halogen lamps with a zenith angle of 30°, located at a distance of approximately 0.50 m from  
17 the soil sample were used as light sources. The soil samples, which were gently pressed and leveled with a  
18 spatula to obtain a smooth surface, were set inside a black cylinder of 10-cm diameter and 1-cm height during  
19 the measurements. The spectroradiometer was located in a nadir position with a distance of 10 cm from the  
20 sample, allowing the radiance measurements within a circular area of approximately 4.5-cm diameter. The noise  
21 level in the spectral signal was reduced through averaging 30 spectra for each soil sample. In addition, to  
22 eliminate any possible spectral anomalies due to geometry of measurement, four replicate scans were acquired  
23 by rotating the soil sample by 90° and were averaged in post-processing. A Spectralon panel (30 × 30 cm<sup>2</sup>,  
24 Labsphere Inc., North Sutton, USA) was used as white reference to compute reflectance values. A reference  
25 spectrum under the same conditions of measurement was acquired immediately before the first scan and after  
26 every set of eight samples.

27 The spectral reflectance curves were finally averaged at 10 nm, so reducing the number of wavelengths from  
28 2151 to 216, to smooth the spectra and keep down the risk of over-fitting (Shepherd and Walsh, 2002).

29 In order to further reduce residual noise and enhance the absorption frequencies, a number of spectral data pre-  
30 processing techniques were applied before statistical analysis:

- 1 • The measured reflectance (R) spectra were transformed into apparent absorbance through  $\log(1/R)$  to  
2 reduce noise, offset effects, and to enhance the linearity between measured absorbance and SOM concentration.
  - 3 • The absorbance spectra were mean-centered to ensure that all results would be interpretable in terms  
4 of variation around the mean.
  - 5 • Subsequently, the absorbance spectra were smoothed through a median filter algorithm with a first  
6 derivative to remove an additive baseline (Viscarra Rossel, 2008).
  - 7 • Finally, absorbance spectra were normalized through the multiplicative scatter correction (MSC) (Geladi  
8 et al., 1985) to reduce the effect of scattering.
- 9  
10 Details on pre-processing methods can be found in Martens and Næs (1989) and in Næs et al. (2004).

#### 11 12 2.4. *Analysis of Vis-NIR data*

13  
14 The approach aims at establishing a mathematical relationship between the response variable  $y$  (measured  
15 values of SOM) and the set of predictors  $X$  (spectral data). Among the available multivariate statistical methods,  
16 partial least squares regression (PLSR) (Geladi and Kowalski, 1986) was preferred. PLSR is a common  
17 chemometrics method in Vis-NIR analysis (Martens and Næs, 1989; Viscarra Rossel et al., 2006). The idea  
18 behind PLSR is to find a few linear combinations (components or factors) of the original  $X$ -values and to use  
19 only these linear combinations in the regression equation (Næs et al., 2004). In this way, the irrelevant and  
20 unstable information is discarded and only the most relevant part of the  $X$ -variation is used for regression; the  
21 problem of collinearity is solved and more stable regression equations obtained (Næs et al., 2004). PLSR reduces  
22 the Vis-NIR matrix (reflectance by observation) to a small number of statistically significant components and is  
23 based on latent variable decomposition of two sets of variables: the set  $X$  of predictors (matrix  $n \times N$ , where  $n$  is  
24 the number of observations and  $N$  is the number of wavelengths) and the set  $y$  of response variable (vector  $n \times 1$   
25 of SOM measurements). The latent variables are orthogonal factors that maximize the covariance between  
26 independent ( $X$ ) and dependent variables ( $y$ ), and explain most of the variations in both predictors and  
27 responses. For more details on the PLSR method, see e.g. Martens and Næs (1989).

28 The optimal number of latent variables was chosen through a leave-one-out cross-validation (Efron and  
29 Tibshirani, 1993) as the number that minimizes the predicted residual sum of squares (PRESS).

30 The best prediction of the leave-one-out cross-validation model was evaluated using the coefficient of

1 determination (R<sup>2</sup>) and root mean square error of prediction (RMSE).  
2 Besides centering the predictors and the response variable, they were also scaled to standard deviation equal to  
3 one. Scaling serves to place all predictors and response on an equal footing relative to their variation in the data.  
4 Pre-treatment of data was performed with PARLeS v. 3.1 software developed by Viscarra Rossel (2008), and  
5 PLSR with the procedure PLS of SAS/STAT statistical package software (SAS Institute Inc., 2013 release 9.3).

6

## 7 2.5. REML-estimation of SOM with spatially correlated errors

8

9 The regression method implemented in the PLS procedure fits the observed data through the use of the ordinary  
10 least squares (OLS) method, which assumes that residuals of prediction are independent and identically  
11 distributed. Since SOM observations are expected to be autocorrelated, the variogram estimated from the  
12 residuals is biased because its point estimates depend in a non-linear way on the estimates of the coefficients of  
13 regressors (Lark et al., 2006). The state of the art for this problem is to use the residual maximum likelihood  
14 (REML) estimation of the spatial variance model in combination with the empirical best linear unbiased  
15 predictor (E-BLUP) (Patterson and Thompson, 1971). According to this approach, SOM is computed from a linear  
16 mixed effect model (LMEM) comprising an additive combination of the factors extracted with PLS as fixed  
17 effects, one random effect, which is the spatially dependent random variable in a geostatistical context and an  
18 independent random variable. The advantage of REML, to estimate variance parameters for the random effect, is  
19 that it reduces the bias found in maximum likelihood or OLS estimates (Cressie, 1993). Spatial covariance  
20 models, originally developed for Geostatistics, are also used in the mixed effect model approach (Diggle et al.,  
21 1998); therefore, correlation structure can be described by a variogram of spatial residuals.

22 The LMEM may be written as:

23

$$24 \quad z = X\beta + Zu + \varepsilon \quad 1$$

25

26 where the vector  $z$  contains the SOM observations,  $X$  is an  $n \times p$  design matrix consisting of the  $n$  observations of  
27 the  $p$  fixed effects (the factors extracted with PLS), the vector  $\beta$  contains the  $p$  fixed-effect coefficients;  $u$  is the  
28 spatially dependent random variable;  $Z$  is the design matrix and the term  $\varepsilon$  is a vector of independent random  
29 errors. The random terms  $u$  and  $\varepsilon$  are assumed to be jointly Gaussian and independent of each other. The term  $\varepsilon$ ,  
30 in particular, represents both independent measurement errors and variation at a spatial scale smaller than the

1 one of sampling and is the nugget effect in geostatistics. If  $u$  is assumed to be drawn from a second-order  
2 stationary random process, its correlation matrix will depend only on the relative locations of the observations,  
3 and its covariance function will be an authorized mathematical model of the distance between observations used  
4 in geostatistics. The parameters of such a function will be estimated by REML because this removes dependence  
5 of the estimates on the fixed-effect coefficients. These coefficients are the ones that maximize the residual log-  
6 likelihood function and are found numerically through the use of a ridge-stabilized Newton–Raphson algorithm  
7 (Lindstrom and Bates, 1988). Once the parameters of covariance function and the coefficients of fixed effects are  
8 estimated, the predictions are computed at the sites where the factors are known.

9 The spatial association of the residuals from PLSR was tested in different ways:

- 10 • Calculating the Moran's  $I$  (Moran, 1950) and Geary's  $c$  (Geary, 1947) spatial autocorrelation statistics  
11 and comparing these to their expected values under a null spatial (completely randomized) model;
- 12 • Fitting a mathematical model to the experimental variogram of the residuals;
- 13 • Performing a likelihood ratio test to assess whether the simplifications used in the non-spatial  
14 correlation model are still applicable with spatially correlated errors (Oman, 1991; Wolfinger, 1993).

15 This test requires computation of the restricted log-likelihood (LLR) for each model, evaluated at the REML  
16 estimates of parameters. The likelihood ratio statistic for comparing the reduced (non-spatial) model to the full  
17 (spatial) model is:

$$18 \chi^2 = -2[\text{LLR}(\text{reduced model}) - \text{LLR}(\text{full model})];$$

21 Under the null hypothesis that the reduced model is no different from the full one; the likelihood ratio statistic is  
22 distributed as Chi-squared with the number of freedom degrees equal to the difference in the number of  
23 parameters of each of the two models. Because the fixed part is the same for the two models, only the number of  
24 parameters in the variance–covariance structure needs to be considered.

25 Since REML estimation entails an explicit assumption that  $\epsilon$  has a Gaussian distribution, the distributional  
26 assumptions for the mixed effect model are tested by calculating the descriptive statistics of residuals and  
27 comparing residuals with the corresponding quantiles of the standard normal variable.

28 The two procedures, PLSR and the combination of PLSR with linear mixed effect model, are also compared by  
29 root mean square prediction error (RMSPE) calculated through cross-validation.

30 The linear mixed effect model approach was implemented using MIXED procedure of SAS/STAT software (SAS



1 Institute Inc., 2013 release 9.3).

2 To form the SOM predictions at an unsampled site in order to produce a continuous map, the estimates were  
3 interpolated by ordinary kriging (Webster and Oliver, 2007). All geostatistical analyses were carried out with the  
4 software package ISATIS®, release 2014 (Géovariances, 2014).

5

### 6 3. *Results and discussion*

7

8 Table 1 presents summary statistics for SOM data. The SOM contents varied spatially from a minimum value of  
9 0.30% to a maximum of 6.50%, with a mean value of 2.62% (Table 1). The SOM dataset was characterized by a  
10 positively skewed distribution (0.84) (Table 1, Fig. 3).

11 To analyze the relationship of SOM with soil type and land use, the measured SOM data were classified into four  
12 classes (i.e. high, medium, low and very low) based on the USDA textural classes (Table 2 and Fig. 2) (Soil Survey  
13 Staff, 2010) and then compared with soil types and land use (Fig. 4).

14 The comparison between the classes of topsoil SOM content and the ones of soil type and land use showed that  
15 high SOM contents were prevalently recorded in the Cambisols and Luvisols (Fig. 4a) and in woodland areas (Fig.  
16 4b). Low SOM content values were measured in topsoil samples of cropland, which are often characterized by  
17 intense water erosion and tillage-induced erosion due to unsustainable agricultural practices (Conforti, 2009).  
18 Moreover, topsoil samples with very low SOM content were associated with barren lands, mostly on land with  
19 intense erosive processes (Conforti et al., 2013a, b).

20 A visual inspection of the set of spectra allowed us to detect that they are affected by variations in SOM content.

21 The mean reflectance spectra of the four classes of SOM content (Fig. 5) showed a tendency to decrease with  
22 SOM, as reported by other authors (Ben-Dor, 2002). The overall shape of the Vis–NIR spectra was generally  
23 similar for all samples and most displayed some degree of steep slope between 400 and 900 nm. All soil  
24 reflectance spectra exhibited high absorption peaks around 1400 nm, 1900 nm and 2200 nm (Fig. 5). These  
25 features may be associated with clay minerals, OH features of free water at 1400 and 1900 nm, and lattice OH  
26 features at 1400 and 2200 nm (Ben-Dor, 2002). The spectra also showed a small absorption peak around 2200  
27 nm, which may be due to organic molecules (e.g., CH<sub>2</sub>, CH<sub>3</sub>, and NH<sub>3</sub>), Si–OH bonds, cation–OH bonds in  
28 phyllosilicate minerals (e.g., kaolinite, montmorillonite) (Clark et al., 1990).

29 We retained eight PLSR factors (latent variables) since they resulted to be significant by cross-validation and  
30 explained more than 80% of variation in both predictors and response. We deemed acceptable a loss of less than

1 20% of the information for the construction of a prediction model of SOM.

2 The spatial autocorrelation of the residuals from PLSR was verified with both Moran's I and Geary's c, tests  
3 (Table 3). The observed Moran's I coefficient (Table 3) was statistically greater (0.217) than the expected value  
4 (- 0.005) indicating a positive spatial autocorrelation of the residuals. The Geary's c index (Table 3) confirmed  
5 the positive spatial autocorrelation of the residuals and was less (0.681) than the expected value (1).

6 An exponential model with a practical range equal to 600 m was fitted to the experimental variogram of  
7 residuals. The non-spatially correlated component (nugget effect) was about twice (0.23%<sup>2</sup>) the structured  
8 component (partial sill = 0.13%<sup>2</sup>), which may be due to the rather coarse sampling scale of soil. The estimated  
9 parameters of the variogram model were used as input values to initialize the iterative procedure of fitting in the  
10 mixed effect model estimator.

11 The REML estimated parameters (partial sill, range, nugget effect) of the exponential model of covariance  
12 function of residuals and the estimates of the intercept ( $\beta_0$ ) and the coefficients ( $\beta_i$ ) of the eight latent variables  
13 (fixed effects) are shown in Table 4. The exponential spatial variance model was preferred to other authorized  
14 variance models on the basis of the residual likelihood, because all the LMEMs had the same fixed-effect  
15 structure.

16 All the fixed effects and residual (nugget effect) were highly significant; the parameters of the covariance  
17 function were significant at a probability level of about 0.10. The weak stochastic component, related to spatial  
18 autocorrelation, was probably due to a too coarse sampling scale. However, the likelihood ratio test:

19

$$20 \chi^2 = -[LLR(\text{nonspatialmodel}) - LLR(\text{spatialmodel})]$$

$$21 = -(-419.9 + 413.4) = 6.5$$

22

23 was significant at probability level of  $p < 0.05$ , which means that the residuals of SOM estimation were spatially  
24 correlated; therefore, the use of the mixed effect model approach after PLS regression is justified and expected to  
25 improve the prediction of SOM.

26 Table 5 shows the summary statistics of the residuals from the fitted LMEM calculated with cross-validation and  
27 Fig. 6 displays the q-q plot. The residuals were symmetrically distributed and showed no evident departure from  
28 the normality assumptions of the model, supporting the assumption of a Gaussian random process  
29 superimposed on an external drift represented by the spectral latent variables. Moreover, the RMSPE of LMEM  
30 was 0.59, smaller than RMSPE found for traditional PLSR model (0.69), which is further evidence of the

1 advantages of the proposed approach.

2 The utility of using reflectance data, synthesized in eight latent variables as fixed effects, for spatial prediction of  
3 SOM was also proved with the Akaike information criterion (Akaike, 1973), which was smaller for the  
4 estimated LMEM compared with the one of the no-external drift models, in which the one fixed effect was an  
5 overall mean (intercept) (419.4 against 913.9).

6 The above results are quite promising; however, the estimated relation between SOM and spectroradiometric  
7 data needs to be tested further across a wider range of soils, characterized by different properties, texture,  
8 parent material and age of landscape, to confirm its wider applicability.

9 To produce a continuous map of LMEM SOM predictions, a bounded isotropic variogram model was estimated,  
10 after checking the occurrence of anisotropy with a variogram map (not shown), including a nugget effect  
11 (1.07%) and two spherical models with ranges of about 753 m and 2066 m, respectively. The results of cross  
12 validation were quite satisfactory because the mean of the estimation error (-0.01%) and the mean squared  
13 deviation ratio (1.06) were close to 0 and 1, respectively.

14 The interpolated map of the LMEM SOM predictions, obtained using ordinary kriging, is reported in Fig. 7. The  
15 map shows that high contents of SOM (N 5%) can be observed along the slopes in the western part of the study  
16 area, which is characterized by Cambisols formed on metamorphic rocks; in addition, the SOM shows higher  
17 values where Fluvisols are developed and with scrub/herbaceous land cover and olive groves. Low values of  
18 SOM (on average about 2%) were mapped in the central and eastern portion of the Turbolo catchment, where there  
19 are Luvisols and Cambisols and land use characterized mainly by crops and olive groves (Fig. 2). In these areas,  
20 the low content of SOM could be due to tillage erosion caused by mechanized agriculture, which promotes the  
21 oxidation of SOM and leads to increased soil erosion (Rasmussen et al., 1998). Spatial distribution of SOM shows  
22 that the low contents were found in the areas where soils (e.g. Vertisols and Fluvisols) developed on clayey and  
23 sandy parent materials (Fig. 1), often truncated by erosive processes (Conforti et al., 2011). Moreover, a visual  
24 inspection of the map shows that the lowest values of SOM are located in hilly barren lands, where clay lithology  
25 outcrops.

26 From what previously shown, it results that, by simply adding two columns of spatial coordinates to reflectance  
27 data and modifying the regression method, it is possible to improve SOM prediction and produce a continuous  
28 representation of SOM spatial variation.

29

#### 30 4. Conclusions

1

2 In this study, a combined method (PLSR-regression with correlated errors) was used with Vis-NIR spectra to  
3 determine organic matter in soil within the context of digital soil mapping. The key objective was to develop an  
4 approach, which accounted for spatial dependence,

5

6 should it occur, whereas it is generally ignored in regression methods. The results showed that the approach  
7 proposed can improve the prediction of SOM and that soil reflectance spectra, if treated with prop- er analytical  
8 procedures, can serve as excellent co-variables for SOM estimation. The proposed methodology could be  
9 incorporated into remote/proximal sensing for digital soil-property mapping by using remotely or proximally  
10 sensed hyperspectral images as exhaustive variables, known at each node of an interpolation grid, where only a  
11 small number of reference measurements would be needed to estimate calibration function. The use of  
12 geostatistical techniques, such as multicollocated cokriging or kriging with external drift (Castrignanò et al.,  
13 2011), could extend SOM prediction to the whole area monitored by the remote or proximal sensor.

14

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16

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19

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1 Figures and Table

2 Fig. 1. Location of the study area and topsoil samples. The lithologic map of study area is also reported

3 Fig. 2. Soil (a) and land use (b) maps. A posting of the measured SOM content values using four classes is also  
4 reported.

5 Fig. 3. Histogram of measured SOM data.

6 Fig. 4. Soil samples distribution in the SOM classes for different soil types (a) and land use (b).

7 Fig. 5. Mean reflectance curves of soils for different classes of SOM.

8 Fig. 6. q-q plot of residuals for the fitted spatial linear mixed effects model.

9 Table 1 - Basic statistics of measured SOM content data.

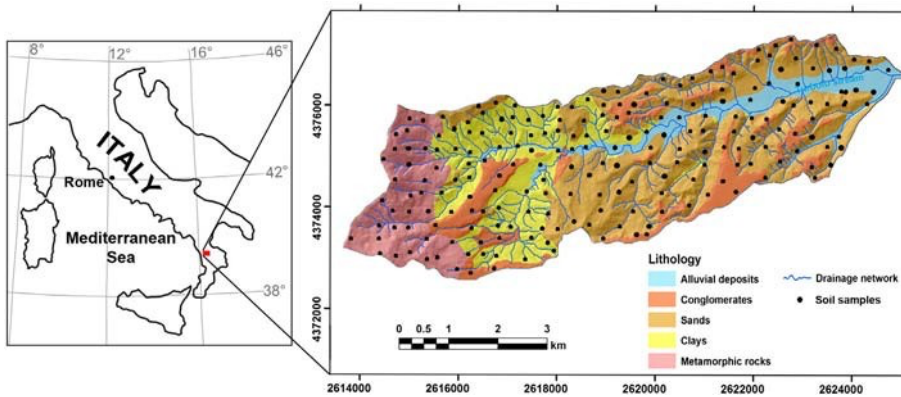
10 Table 2 - SOM content classified according to the USDA textural classes.

11 Table 3 - Results for the autocorrelation statistics.

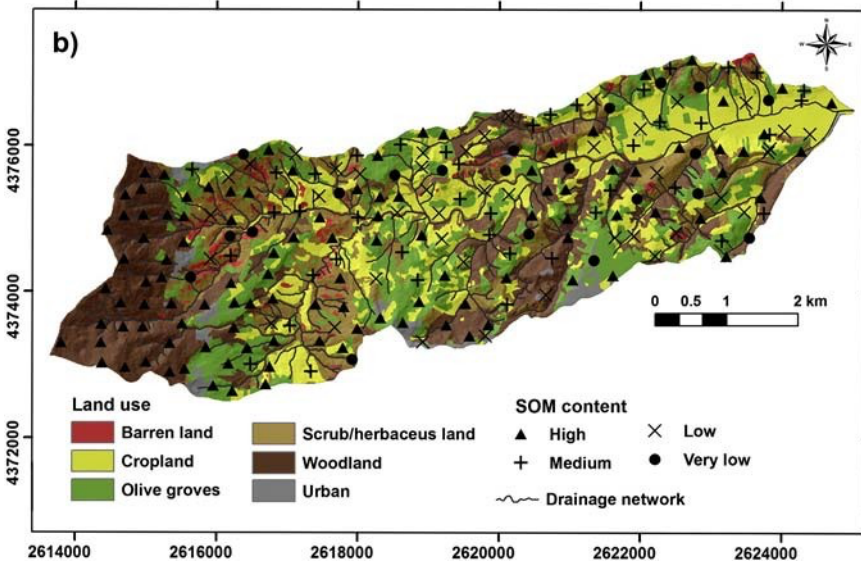
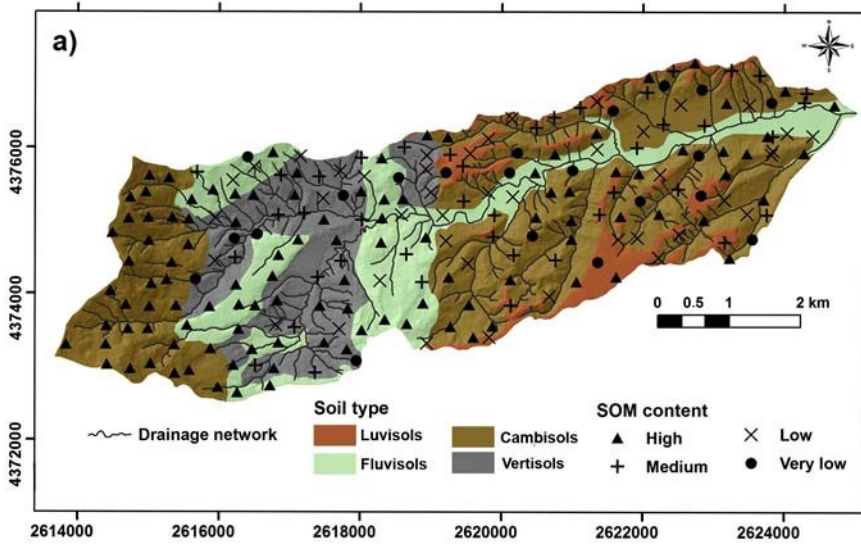
12 Table 4 - Results of linear mixed model estimation.

13 Table 5 - Basic statistics of residuals for the fitted spatial linear mixed effects model.

14

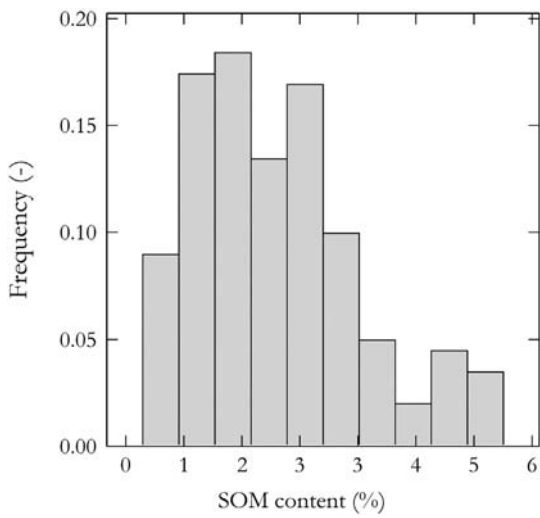


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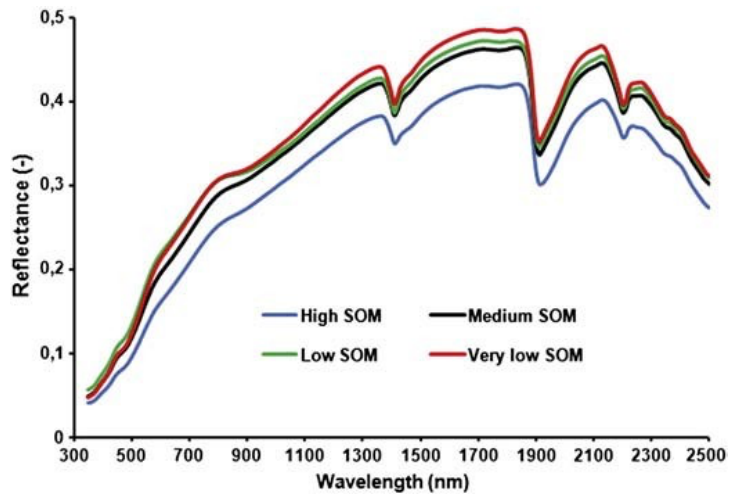
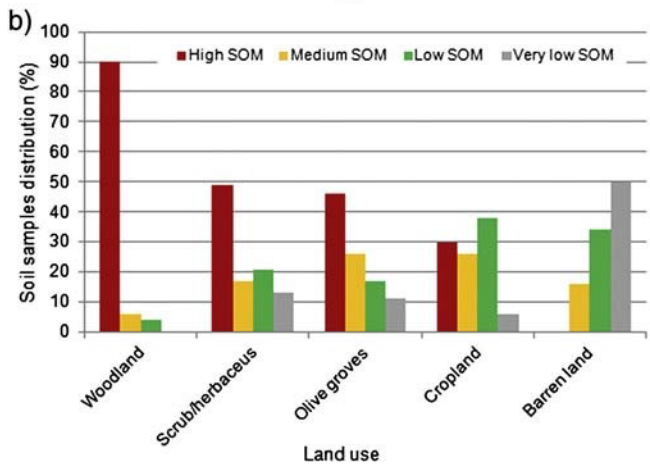
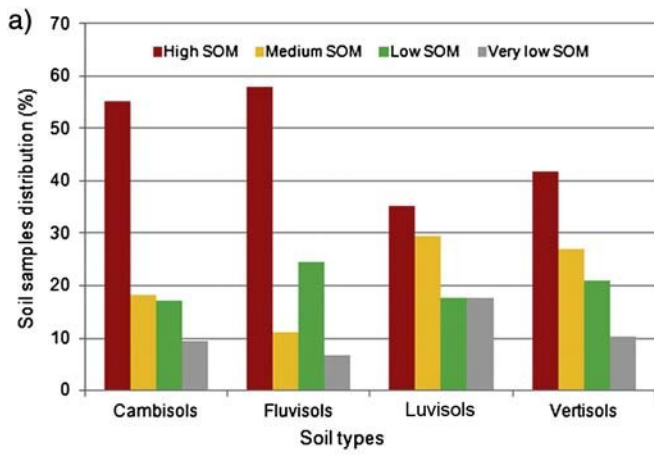


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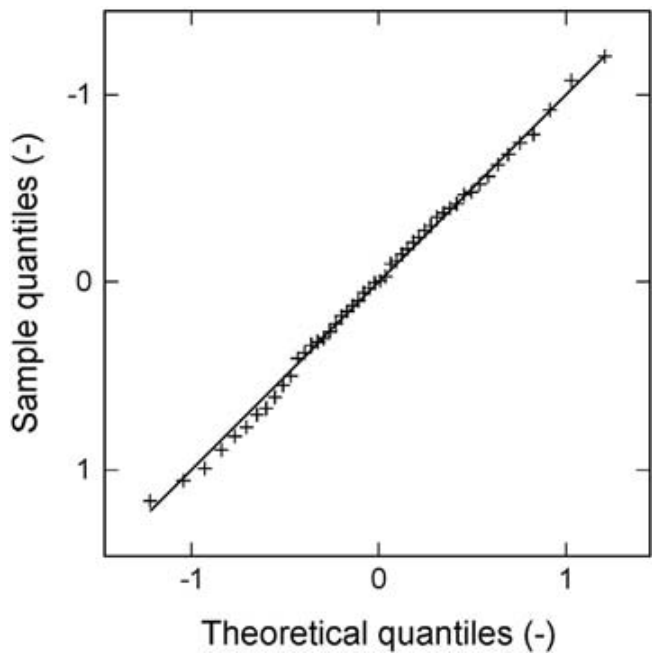


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1

Count	201
Mean (%)	2.62
Minimum (%)	0.30
Lower quantile (%)	1.50
Median (%)	2.40
Upper quantile (%)	3.30
Maximum (%)	6.50
Standard deviation (%)	1.43
Variance (%)	2.04
Skewness (-)	0.84

2

Assumption	Coefficient	Observed	Expected	Stand. dev.	Probability
Randomization	Moran's <i>I</i>	0.217	-0.005	0.049	<0.0001
Randomization	Geary's <i>c</i>	0.681	1.000	0.061	<0.0001

3

USDA texture class	SOM content (%)			
	Very low	Low	Medium	High
Sand, loamy sand, sandy loam	<0.8	0.8-1.4	1.5-2.0	>2.0
Loam, sandy clay, sandy clay loam, silty loam, silt	<1.0	1.0-1.8	1.9-2.5	>2.5
Clay, clay loam, silty clay, silty clay loam	<1.2	1.2-2.2	2.3-3.0	>3.0

4

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Covariance parameter estimates

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Covariance parameters	Subject	Estimate	Standard error	Probability
Exponential model	Partial sill	0.1117	0.1029	0.1389
	Range	377.99	348.72	0.1392
Residual	Nugget effect	0.2552	0.1040	0.0071

Solution for fixed effects

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Effect	Estimate	Standard error	Probability
$\beta_0$	2.6255	0.0639	<0.0001
$\beta_1$	0.1548	0.0068	<0.0001
$\beta_2$	0.0538	0.0070	<0.0001
$\beta_3$	0.1690	0.0154	<0.0001
$\beta_4$	0.0521	0.0088	<0.0001
$\beta_5$	0.0375	0.0074	<0.0001
$\beta_6$	0.0761	0.0133	<0.0001
$\beta_7$	0.1326	0.0191	<0.0001
$\beta_8$	0.1115	0.0219	<0.0001

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1

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Count	201
Mean (%)	-0.01
Minimum (%)	-1.47
Median (%)	0.00
Maximum (%)	1.50
Standard deviation (%)	0.59

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2

3